Curry





A Tasty dish?

Haskell Curry

Curried Functions

- Currying is a functional programming technique that takes a function of N arguments and produces a related one where some of the arguments are fixed
- In Scheme
 - (define add1 (curry + 1))
 - (define double (curry * 2))

A tasty dish?

- Currying was named after the Mathematical logician Haskell Curry (1900-1982)
- Curry worked on combinatory logic ...
- A technique that eliminates the need for variables in <u>mathematical logic</u> ...
- and hence computer programming!
 At least in theory
- The functional programming language <u>Haskell</u> is also named in honor of Haskell Curry

Functions in Haskell



- In Haskell we can define g as a function that takes two arguments of types a and b and returns a value of type c like this:
 - -g::(a, b) -> c
- We can let f be the curried form of g by
 - $-f = \underline{\text{curry}} g$
- The function f now has the signature
 - -f :: a -> b -> c
- f takes an arg of type a & returns a function that takes an arg of type b & returns a value of type c

Functions in Haskell

- All functions in Haskell are curried, i.e., all Haskell functions take just single arguments.
- •This is mostly hidden in notation, and is not apparent to a new Haskeller
- •Let's take the function <u>div</u> :: <u>Int</u> -> <u>Int</u> -> <u>Int</u> which performs integer division
- •The expression div 11 2 evaluates to 5
- •But it's a two-part process
- -div 11 is evaled & returns a function of type Int -> Int
- -That function is applied to the value 2, yielding 5

Note on lambda syntax

- (lambda X (foo X)) is a way to define a lambda expression that takes any number of arguments
- In this case X is bound to the list of the argument values, e.g.:

Currying in Scheme

- Scheme has an explicit built in function, curry, that takes a function and some of its arguments and returns a curried function
- For example:
 - -(define add1 (curry + 1))
 - -(define double (curry * 2))

Simple example (a)

- Compare two lists of numbers pair wise:
 (apply and (map < '(0 1 2 3) '(5 6 7 8)))
- Note that (map < '(0 1 2 3) '(5 6 7 8)) evaluates to the list (#t #t #t #t)
- Applying and to this produces the answer, #t

Simple example (b)

- Is every number in a list positive?
 (apply and (map < 0 ' (5 6 7 8)))
- This is a nice idea, but will not work

map: expects type cyroper list> as 2nd argument, given: 0; other arguments were: #rocedure:<> (5 6 7 8)

=== context ===

/Applications/PLT/collects/scheme/private/misc.ss:74:7

 Map takes a function and <u>lists</u> for each of its arguments

Simple example (c)

- Is every number in a list positive?
- Use (lambda (x) (< 0 x)) as the function (apply and (map (lambda (x) (< 0 x)) '(5 6 7 8)))
- This works nicely and gives the right answer
- What we did was to use a general purpose, two-argument comparison function (?<?) to make a narrower one-argument one (0<?)

Simple example (d)

- Here's where curry helps (curry < 0) ≈ (lambda (x) (< 0 x))
- So this does what we want (apply and (map (curry < 0) '(5 6 7 8)))
- Currying < with 0 actually produces (lambda x (apply < 0 x))
- So (curry < 0) takes one or more args, e.g. ((curry < 0) 10 20 30) => #t ((curry < 0) 10 20 5) => #f

A real world example

- I wanted to adapt a Lisp example by Google's <u>Peter Norvig</u> of a simple program that generates random sentences from a context free grammar
- It was written to take the grammar and start symbol as global variables ☺
- I wanted to make this a parameter, but it made the code more complex ⊗ ⊗
- Scheme's curry helped solve this!

```
#lang scheme

;;; This is a simple ...

(define grammar

'((S -> (NP VP) (NP VP) (NP VP) (S CONJ S))

(NP -> (ARTICLE ADJS? NOUN PP?))

(VP -> (VERB NP) (VERB NP) (VERB NP) VERB)

(ARTICLE -> the the the a a a one every)

(NOUN -> man ball woman table penguin student book dog worm computer robot )

...

(PP -> (PREP NP))

(PP? -> () () () () PP)

))
```

```
#lang scheme

;;; This is a simple ...

(define grammar

'((S -> (NP VP) (NP VP) (NP VP) (NP VP) (S CONJ S))

(NP -> (ARTICLE ADJS? NOUN PP?))

(VP -> (VERB NP) (VERB NP) (VERB NP) VER

(ARTICLE -> the the the a a a one every)

(NOUN -> man ball woman table penguin s
dog worm computer robot)

...

(PP -> (PREP NP))

(PP? -> () () () () PP)

() is like ɛ in a rule, so
80% of the time it => NP VP and
20% of the time it => NP VP and
20% of the time it => NP VP and
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20% of the time it => NP VP and
20% of the time it => NP VP and
20% of the time it => NP VP and
20% of the time it is a conjoined sentence, S CONJ S
```

```
cfg1.ss
scheme> scheme
Welcome to MzScheme v4.2.4 ...
                                                  session
> (require "cfg1.ss")
> (generate 'S)
(a woman took every mysterious ball)
> (generate 'S)
(a blue man liked the worm over a mysterious woman)
> (generate 'S)
(the large computer liked the dog in every mysterious student in the
  mysterious dog)
> (generate 'NP)
(a worm under every mysterious blue penguin)
> (generate 'NP)
(the book with a large large dog)
```

```
(define (generate phrase)
 ;; generate a random sentence or ph
 (cond ((list? phrase)
        (apply append (map generate phrase)))
       ((non-terminal? phrase)
       (generate (random-element (rewrites phrase)))
       (else (list phrase))))
(define (non-terminal? x)
 ;; True iff x is a on-terminal in grammar
 (assoc x grammar))
(define (rewrites non-terminal)
 ;; Return a list of the possible rewrites for non-terminal in grammar
 (rest (rest (assoc non-terminal grammar))))
(define (random-element list)
 ;; returns a random top-level element from list
 (list-ref_list (random (length list))))
```

Parameterizing generate

- Let's change the package to not use global variables for grammar
- The generate function will take another parameter for the grammar and also pass it to non-terminal? and rewrites
- While we are at it, we'll make both parameters to generate optional with appropriate defaults

```
(define default-grammar '((S -> (NP VP) (NP VP) (NP VP) (NP VP)) ...))
                                                                   cfg2.ss
(define default-start 'S)
(define (generate (grammar default-grammar) (phrase default-start))
;; generate a random sentence or phrase from grammar
(cond ((list? phrase)
       (apply append (map generate phrase)))
       ((non-terminal? phrase grammar)
       (generate grammar (random-element
                                                writes phrase grammar))))
       (else (list phrase)))))
(define (non-terminal? x grammar)
;; True iff x is a on-terminal in grammar
(assoc x grammar))
(define (rewrites non-terminal grammar)
;; Return a list of the possible rewrites for non-terminal in grammar
(rest (rest (assoc non-terminal grammar))))
```

```
(define default-grammar '((S -> (NP VP) (NP VP) (NP VP) (NP VP)) ...))
                                                                   cfg2.ss
(define default-start 'S)
(define (generate (grammar default-grammar) (phrase default-start))
;; generate a random sentence or phrase from grammar
(cond ((list? phrase)
       (apply append (map (curry generate grammar) phrase)))
       ((non-terminal? phrase grammar)
        (generate grammar (random-element (rewrites phrase grammar))))
       (else (list phrase)))))
(define (non-terminal? x grammar)
;; True iff x is a on-terminal in grammar
(assoc x grammar))
(define (rewrites non-terminal grammar)
;; Return a list of the possible rewrites for non-terminal in grammar
(rest (rest (assoc non-terminal grammar))))
```

Curried functions

- Curried functions have lots of applications in programming language theory
- The curry operator is also a neat trick in our functional programming toolbox
- You can add them to Python and other languages, if the underlying language has the right support