

Bottom Up Parsing

Motivation

• In the last lecture we looked at a table driven, top-down parser

-A parser for LL(1) grammars

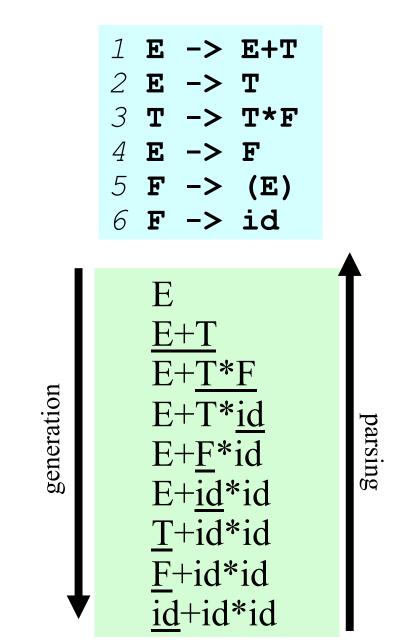
• In this lecture, we'll look a a table driven, bottom up parser

-A parser for LR(1) grammars

• In practice, bottom-up parsing algorithms are used more widely for a number of reasons

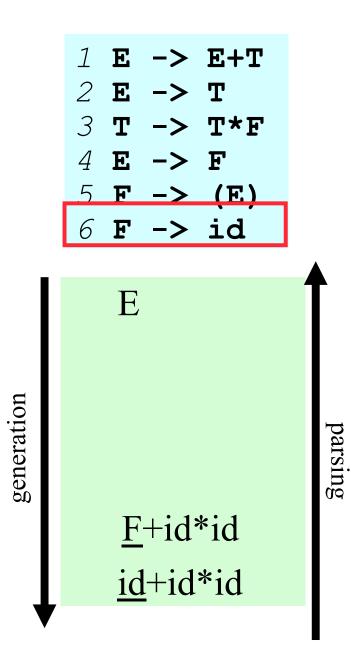
Right Sentential Forms

- Recall the definition of a derivation and a rightmost derivation
- Each of the lines is a (right) sentential form
- A form of the parsing problem is finding the correct RHS in a rightsentential form to reduce to get the previous rightsentential form in the derivation



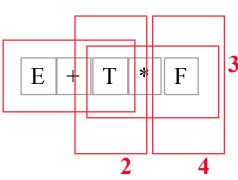
Right Sentential Forms Consider this example

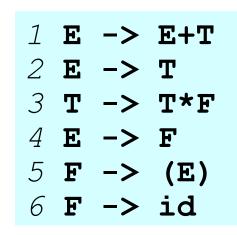
- We start with id+id*id
- What rules can apply to some portion of this sequence?
 - Only rule 6: F -> id
- Are there more than one way to apply the rule?
 - Yes, three
- Apply it so the result is part of a "right most derivation"
 - If there is a derivation, there is a right most one
 - If we always choose that, we can't get into trouble

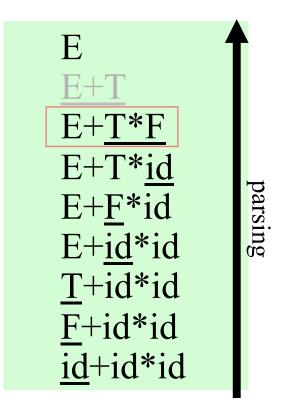


Bottom up parsing

- A bottom up parser looks at a sentential form and selects a contiguous sequence of symbols that matches the RHS of a grammar rule, and replaces it with the LHS
- There might be several 1 choices, as in the sentential form E+T*F
- Which one should we choose?

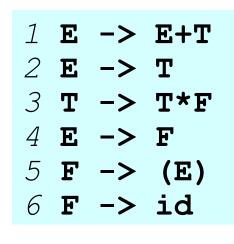


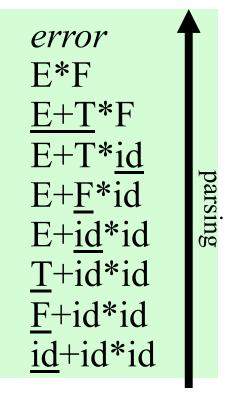




Bottom up parsing

- •If the wrong one is chosen, it leads to failure
- •E.g.: replacing E+T with E in E+T*F yields E+F, which can't be further reduced using the given grammar
- The handle of a sentential form is the RHS that should be rewritten to yield the next sentential form in the <u>right</u> <u>most derivation</u>

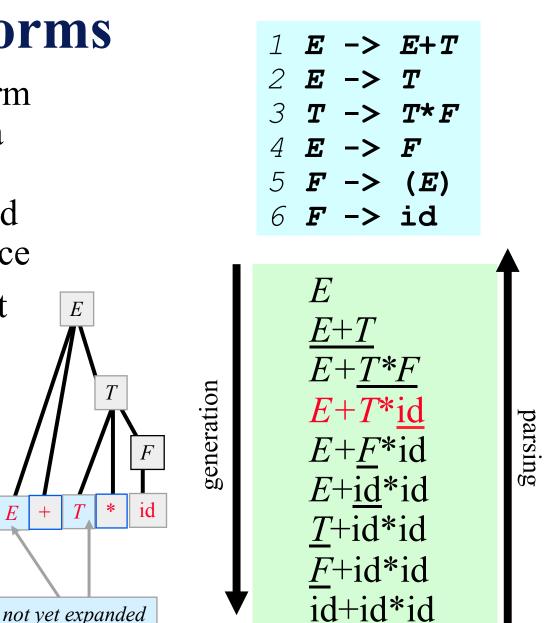




Sentential forms

E

- Think of a sentential form as one of the entries in a derivation that begins with the start symbol and ends with a legal sentence
- It's like a sentence but it may have *unexpanded* non-terminals
- We can also think of it as a parse tree where some leaves are as yet unexpanded nonterminals



Handles

- A handle of a sentential form is a substring α such that :
 - a matches the RHS of some production A -> α ; and
 - replacing α by the LHS A represents a step in the reverse of a rightmost derivation of s.
- For this grammar, the rightmost derivation for the input abbcde is
 S => aABe => aAde => aAbcde => abbcde

1:	S	->	aABe Abc b d
2:	Α	->	Abc
3:	Α	->	b
4:	В	->	d

• The string **aAbcde** can be reduced in two ways:

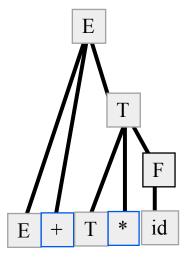
(1) aAbcde => aAde (using rule 2)

(2) aAbcde => aAbcBe (using rule 4)

- But (2) isn't a rightmost derivation, so Abc is the only handle.
- Note: the string to the right of a handle will only contain terminals (why?)

Phrases

- A **phrase** is a subsequence of a sentential form that is eventually "reduced" to a single non-terminal.
- A **simple phrase** is a phrase that is reduced in a single step.
- The **handle** is the leftmost simple phrase.

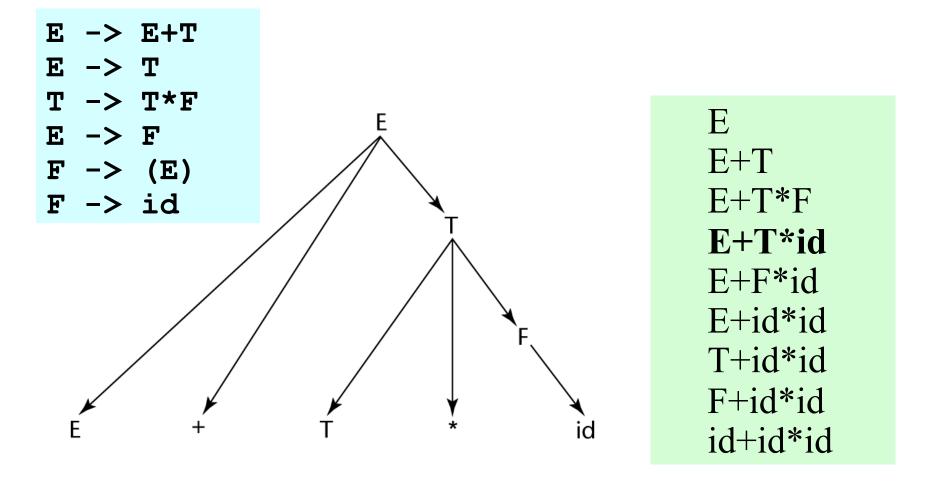


For sentential form E+T*id what are the •phrases: E+T*id, T*id, id •simple phrases: id •handle: id

Phrases, simple phrases and handles

- **Def:** β is the *handle* of the right sentential form $\gamma = \alpha\beta w$ if and only if S =>*rm $\alpha Aw => \alpha\beta w$
- Def: β is a *phrase* of the right sentential form γ if and only if S =>* $\gamma = \alpha 1 A \alpha 2 =>+ \alpha 1 \beta \alpha 2$
- Def: β is a *simple phrase* of the right sentential form γ if and only if S =>* $\gamma = \alpha 1 A \alpha 2 => \alpha 1 \beta \alpha 2$
- The handle of a right sentential form is its leftmost simple phrase
- Given a parse tree, it is now easy to find the handle
- Parsing can be thought of as handle pruning

Phrases, simple phrases and handles



On to shift-reduce parsing

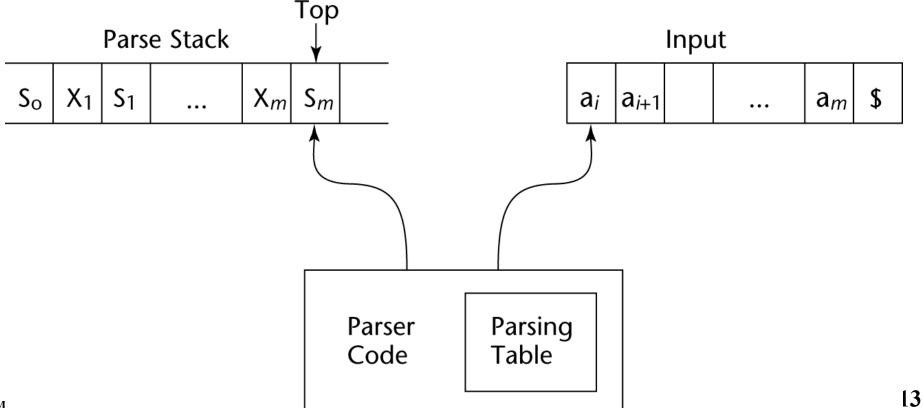
- How to do it w/o having a parse tree in front of us?
- Look at a shift-reduce parser the kind that *yacc* uses
- A shift-reduce parser has a queue of input tokens & an initially empty stack. It takes one of 4 possible actions:
 - -Accept: if the input queue is empty and the start symbol is the only thing on the stack
 - -Reduce: if there is a handle on the top of the stack, pop it off and replace it with the rule's RHS
 - -Shift: push the next input token onto the stack
 - -Fail: if the input is empty and we can't accept
- In general, we might have a choice of (1) shift, (2) reduce, or (3) maybe reducing using one of several rules
- The algorithm we next describe is deterministic

Shift-Reduce Algorithms

A shift-reduce parser scans input, at each step decides to:

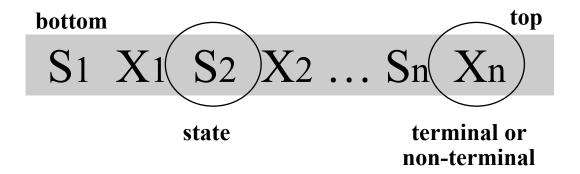
•Shift next token to top of parse stack (along with state info) or

•Reduce the stack by POPing several symbols off the stack (& their state info) and PUSHing the corresponding non-terminal (& state info)

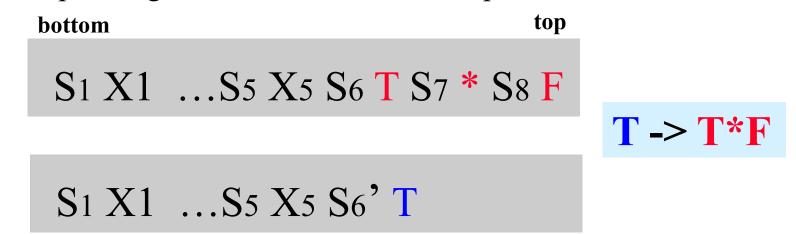


Shift-Reduce Algorithms

The stack is always of the form



• A reduction step is triggered when we see the symbols corresponding to a rule's RHS on the top of the stack



LR parser table

LR shift-reduce parsers can be efficiently implemented by precomputing a table to guide the processing

	Action						Goto		
State	id	+	*	()	\$	E	Т	F
0	S5		S4				1	2	3
1		S6				accept			
2		R2	S7		R2	R2			
3		R4	R4		R4	R4			
4	\$5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

More on this Later . . .

When to shift, when to reduce

- Key problem in building a shift-reduce parser is deciding whether to shift or to reduce
 - repeat: *reduce* if a handle is on top of stack, *shift* otherwise
 - Succeed if there is only S on the stack and no input
- A grammar may not be appropriate for a LR parser because there are <u>conflicts</u> which can not be resolved
- Conflict occurs when the parser can't decide whether to:
 - shift or reduce the top of stack (a shift/reduce conflict), or
 - reduce the top of stack using one of two possible productions (a reduce/reduce conflict)
- There are several varieties of LR parsers (LR(0), LR(1), SLR and LALR), with differences depending on amount of lookahead and on construction of the parse table

Conflicts

Shift-reduce conflict: can't decide whether to shift or to reduce

- Example : "dangling else"
 Stmt -> if Expr then Stmt

 | if Expr then Stmt else Stmt
 | ...
- What to do when else is at the front of the input?

Reduce-reduce conflict: can't decide which of several possible reductions to make

• Example :

```
Stmt -> id ( params )
| Expr := Expr
| ...
```

Expr -> id (params)

• Given the input a(i, j) the parser does not know whether it is a procedure call or an array reference.

LR Table

- An LR configuration stores the state of an LR parser (S0X1S1X2S2...XmSm, aiai+1...an\$)
- LR parsers are table driven, where the table has two components, an ACTION table and a GOTO table
- The ACTION table specifies the action of the parser (shift or reduce) given the parser state and next token

-Rows are state names; columns are terminals

• The GOTO table specifies which state to put on top of the parse stack after a reduce

-Rows are state names; columns are non-terminals

	[1		1	1
	Action									
State	id	+	*	()	\$	E	Т	F	
0	\$5		S4				1	2	3	
If in sta	te 0 and	S6				accept				
id, then		R2	S7		If in state					
and go	to state 5	R4	R4		no more we are do	one R4				
4	\$5			S4			8	2	3	
5		R6	R6		R6	R6				
6	If in state 5 a			S4				9	3	
7	is *, then RE 6. Use goto	able and	exposed	S4					10	
8	state to selec	t next sta So	te		S11			1	: E -	 -> E+T
9		R1	S7		R1	R1		2	2: E -	-> T
10		R3	R3		R3	R3				-> T*F -> F
11		R5	R5		R5	R5			5: F - 5: F -	-> (E)
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Parser actions

Initial configuration: (S0, a1...an\$)

Parser actions:

- 1 If ACTION[Sm, ai] = Shift S, the next configuration is: (S0X1S1X2S2...XmSmaiS, ai+1...an\$)
- 2 If ACTION[Sm, ai] = Reduce $A \rightarrow \beta$ and S = GOTO[Sm-r, A], where r = the length of β , the next configuration is

(S0X1S1X2S2...Xm-rSm-rAS, aiai+1...an\$)

- 3 If ACTION[Sm, ai] = Accept, the parse is complete and no errors were found
- 4 If ACTION[Sm, ai] = Error, the parser calls an errorhandling routine

Example

1:	Ε	->	E+T
2:	Ε	->	Т
3:	Т	->	T*F
4:	Т	->	F
5:	F	->	(E)
6:	F	->	id

Stack	Input	action		
0	Id + id * id \$	Shift 5		
0 id 5	+ id * id \$	Reduce 6 goto(0,F)		
0 F 3	+ id * id \$	Reduce 4 goto(0,T)		
0 Т 2	+ id * id \$	Reduce 2 goto(0,E)		
0 E 1	+ id * id \$	Shift 6		
0 E 1 + 6	id * id \$	Shift 5		
0 E 1 + 6 id 5	* id \$	Reduce 6 goto(6,F)		
0 E 1 + 6 F 3	* id \$	Reduce 4 goto(6,T)		
0 Е 1 + 6 Т 9	* id \$	Shift 7		
0 Е 1 + 6 Т 9 * 7	id \$	Shift 5		
0 E 1 + 6 T 9 * 7 id 5	\$	Reduce 6 goto(7,E)		
0 E 1 + 6 T 9 * 7 F 10	\$	Reduce 3 goto(6,T)		
0 Е 1 + 6 Т 9	\$	Reduce 1 goto(0,E)		
0 E 1	\$	Accept		

	Action						Goto		
State	id	+	*	()	\$	E	Т	F
0	S5		S4				1	2	3
1		S6				accept			
2		R2	S7		R2	R2			
3		R4	R4		R4	R4			
4	\$5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	\$5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

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Yacc as a LR parser

- The Unix yacc utility is just such a parser.
- It does the heavy lifting of computing the table
- To see the table information, use the –v flag when calling yacc, as in

yacc –v test.y

```
0 $accept : E $end
1 E : E '+' T
2 | T
3 T : T '*' F
4 | F
5 F : '(' E ')'
6 | "id"
```

```
state O
```

```
$accept : . E $end
                             (0)
             shift 1
        '('
        "id"
              shift 2
           error
        E goto 3
        T goto 4
        F
           goto 5
state 1
        F: '('. E')'
                          (5)
        '('
             shift 1
        "id"
              shift 2
           error
        E goto 6
        T goto 4
        F
           goto 5
```